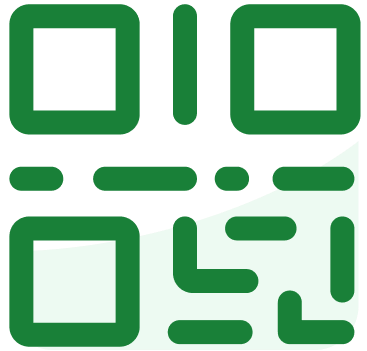


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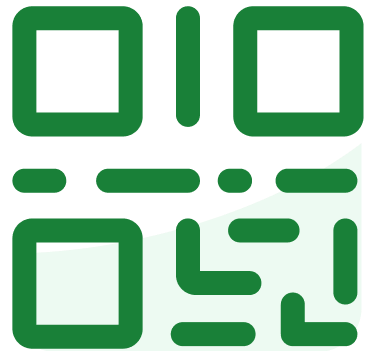
Introduction to Quantum Programming

양자정보 겨울학교

2024.1.14 - 1.19

성균관대학교 김준기

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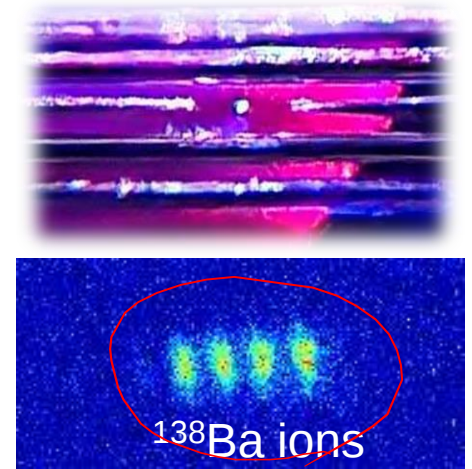
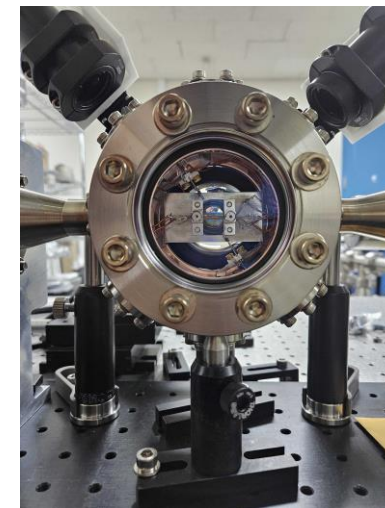
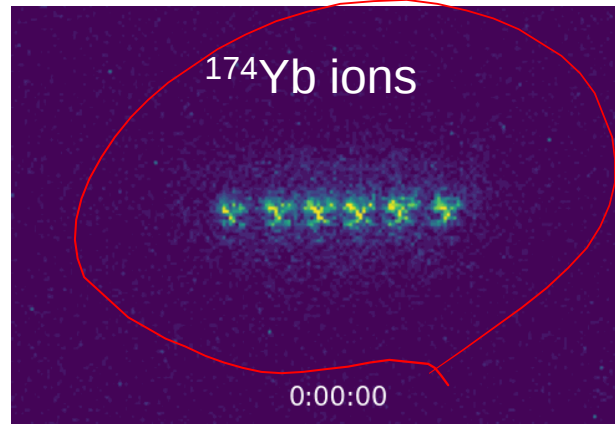
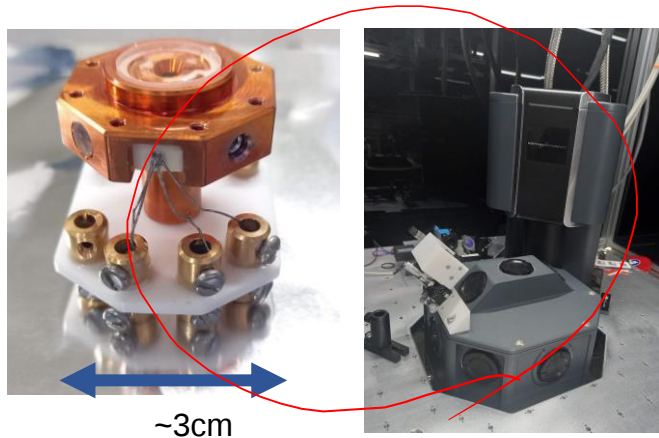


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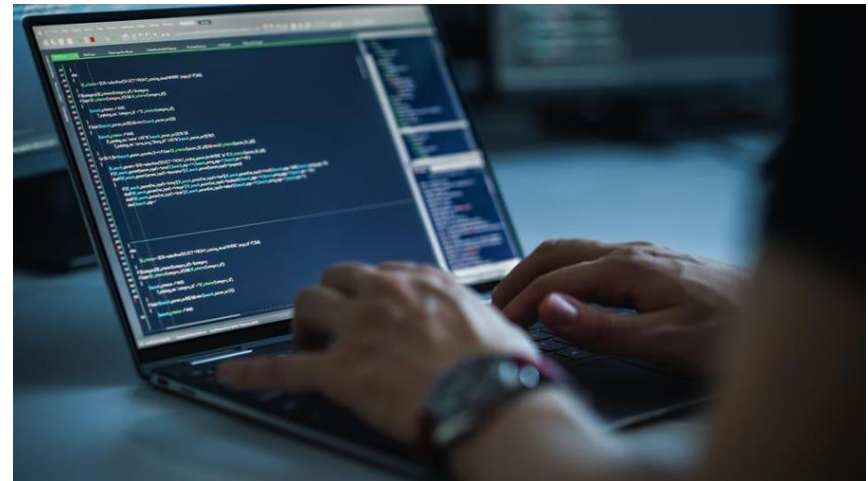
Speaker : Prof. Junki Kim

- Quantum Engineering with Trapped Ions (QuETI) Lab. @ SKKU
- Research Topics
 - Full-stack Ion-trap Quantum Computing
 - Quantum engineering for scalable & versatile QI platform
 - Ion-photon quantum interface
 - High-dimensional quantum information processor



Quantum Programming?

- Programming : the composition of sequences of *instructions*, that computers can follow to perform tasks.
 - Classical computers use **bits** (0 or 1).
 - Bits follows **Boolean algebra**
- Quantum programming – set of *quantum instructions*
 - Quantum computers use **qubits**
 - Instructions for qubits? Algebra for qubits?

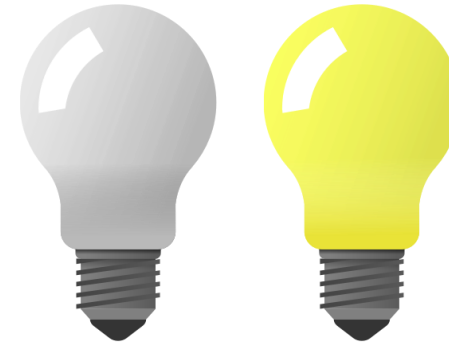


Contents

- Classical computing – logic circuits
- Quantum information basics – Qubits
- Quantum gates and Quantum circuits
- Quantum computing architectures

Bits

- The minimal unit of information
- Ex) Head/Tail of coins, Lamp on/off

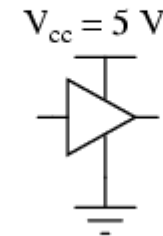
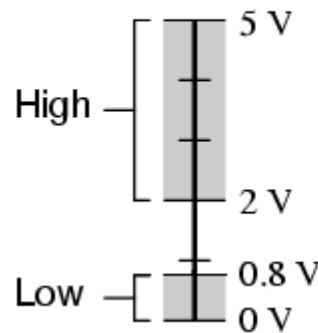


- Number of possible states with N bits : 2^N
- 1 byte = 8 bits

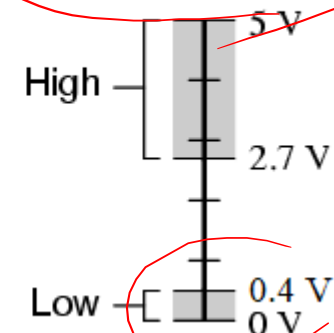
Other than bits?

- Dice (Cubic) : 6^N
- DNA : A,G,C,T = 4 Nucleobase
- Why bits? : Easy to physically realize (no intermediate state), Resilient to noise.
- ex) TTL (Transistor-transistor logic)

*Acceptable TTL gate
input signal levels*



*Acceptable TTL gate
output signal levels*

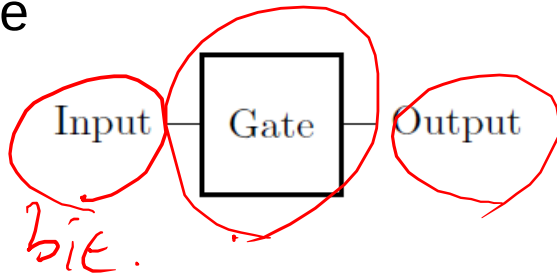


Encoding informations

- ASCII
 - Use 7 bits to encode various characters and signals
 - 65 = 100 0001 (2) = "A"
 - 48 = 011 0000 (2) = "0"
 - 95 bit string → character/number/special characters - printable, 32 bit string → Control character
- UTF-8 / Unicode
 - Up to 32 bits (4-byte) : $2^{32} = 4,294,967,296$ states
 - In use : 1,112,064
 - All other language characters (including Korean) need unicode

Logic gate ← Instruction

- Computers store information in bit format.
- Computer calculation = bit calculation
- Single bit gate

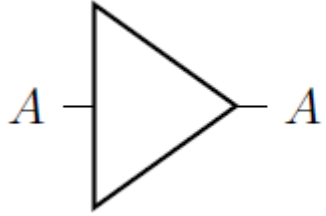


Input	Output
0	?
1	?

0 1
0 1

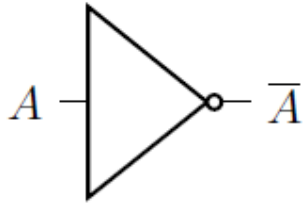
Single bit gate

- Identity gate



A	A
0	0
1	1

- NOT gate

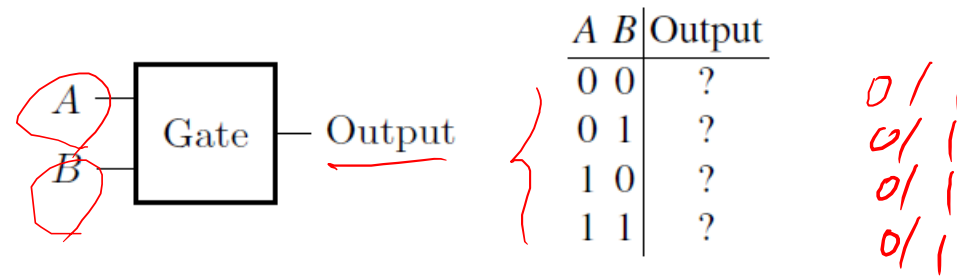


A	$\bar{A}$
0	1
1	0

- Always 0 gates , Always 1 gates

Two-bit gate

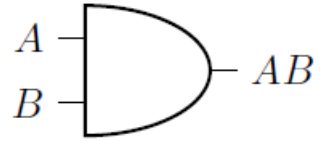
- Input bits = 2, output bit = 1 $\rightarrow 2^4 = 16$ cases



- Notable two-bit gates : AND, OR, XOR, NAND, NOR

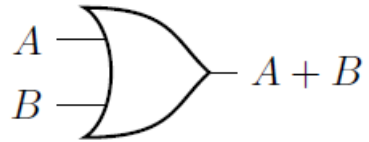
Two-bit gates

- AND gate



A	B	AB
0	0	0
0	1	0
1	0	0
1	1	1

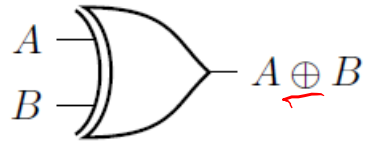
- OR gate



A	B	$A + B$
0	0	0
0	1	1
1	0	1
1	1	1

Two-bit gates

- XOR gate



$A \neq B$

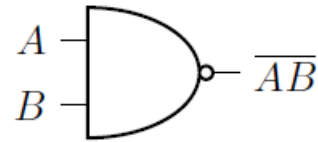
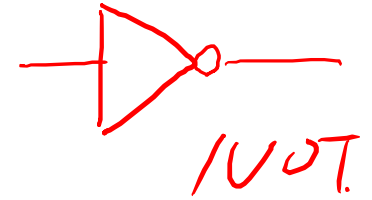
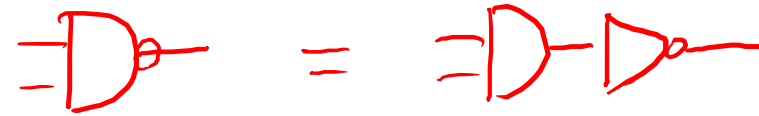
A	B	$A \oplus B$
0	0	0
0	1	1
1	0	1
1	1	0

0
1
1
2. 1. (or)

- Modulo 2 addition : $\oplus$, $1 + 1 \pmod{2} = 2 \pmod{2} = \underline{0 \pmod{2}}$

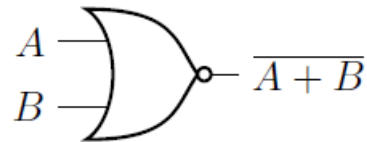
Two-bit gates

- ~~N~~AND gate ↗ NOT



A	B	$\overline{AB}$
0	0	1
0	1	1
1	0	1
1	1	0

- NOR gate

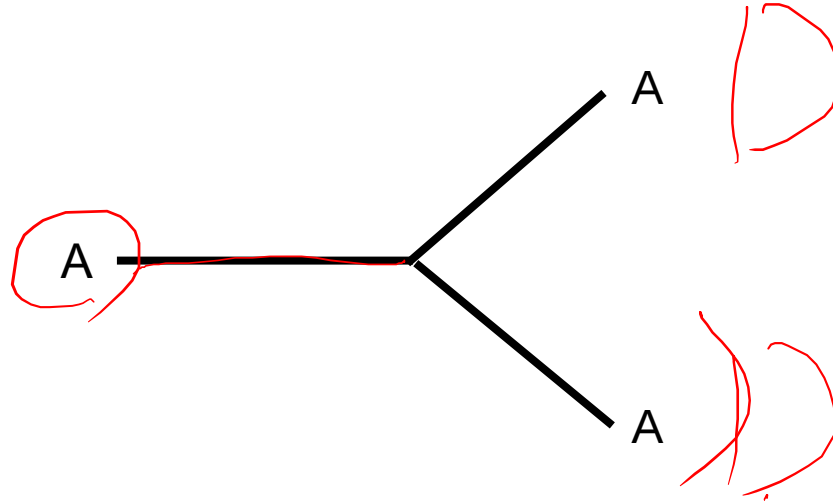


A	B	$\overline{A+B}$
0	0	1
0	1	0
1	0	0
1	1	0



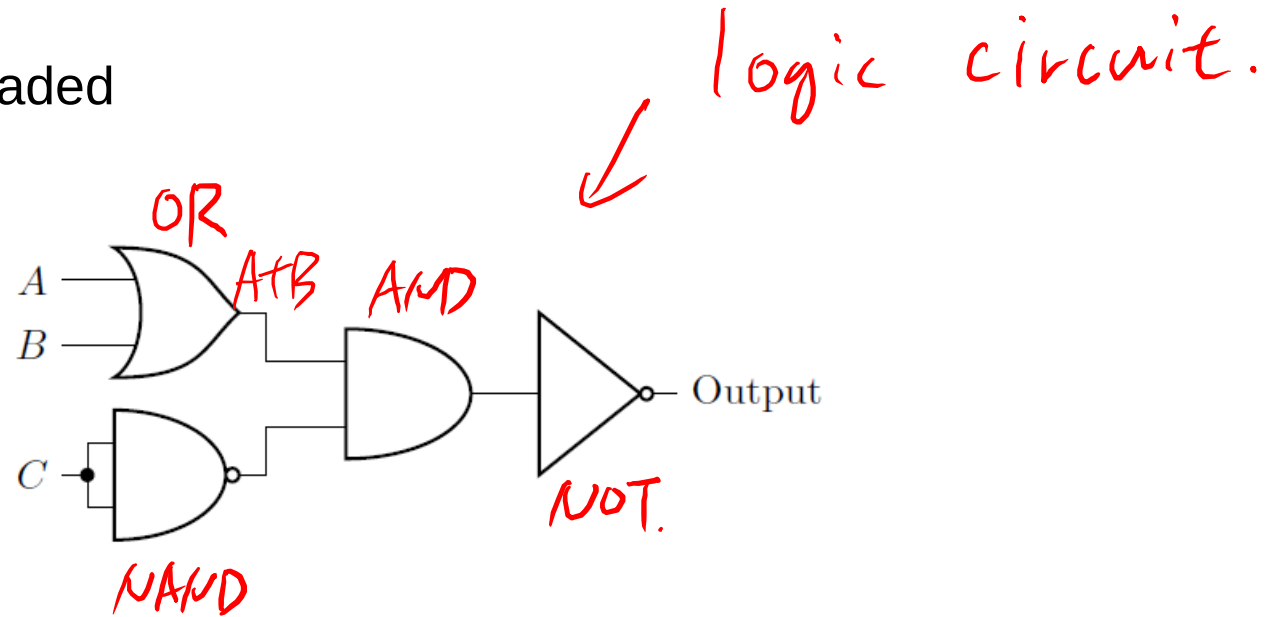
Fan out (copy)

- Copy information (Fan out)



Composite logic gates

- Multiple logic gates can be cascaded



Universal Logic gate

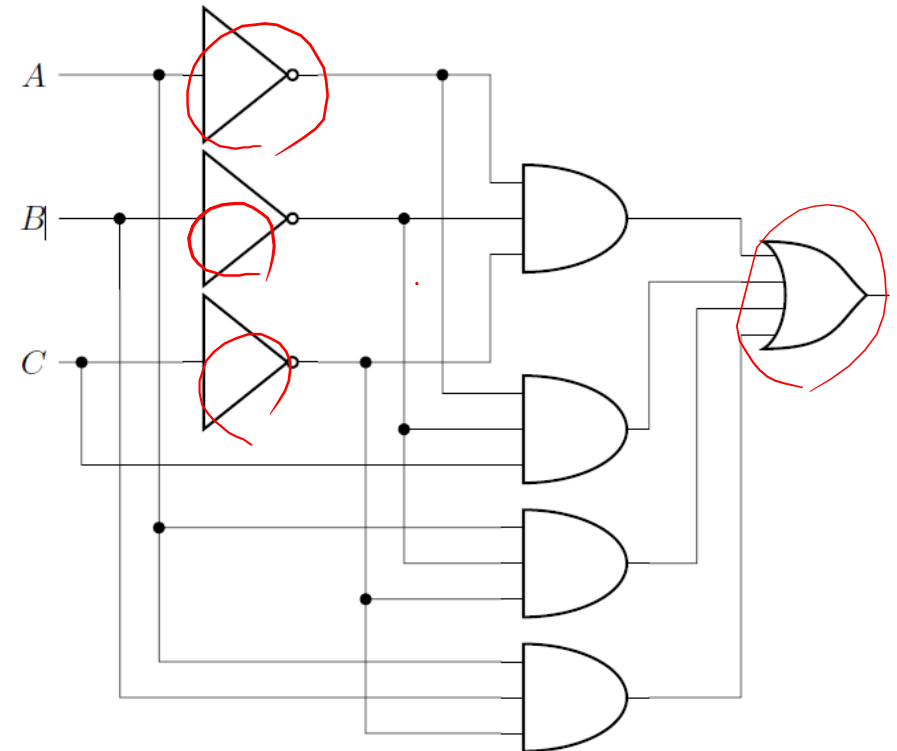
$$f(x) = x^2 + 3x + 2$$

- To realize arbitrary logical operation $f(A, B, C, \dots) = A'$, How many logic gates are required?
 - Possible input bitstrings $2^N \rightarrow 2^N$ different logic gates required? Fortunately not!
 - arbitrary logic operations can be decomposed into AND, OR, NOT gates
 - $\rightarrow$ {AND, OR, NOT} is 'Universal logic gate set'

A	B	C	Output
0	0	0	1
0	0	1	1
0	1	0	0
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	1
1	1	1	0

$$\begin{aligned} \bar{A} \cdot \bar{B} \cdot \bar{C} &\rightarrow 1 \text{ only if} \\ + \bar{A} \cdot \bar{B} \cdot C &\rightarrow 1 \text{ ''} \\ + A \cdot \bar{B} \cdot \bar{C} \\ + A B \bar{C} \end{aligned}$$

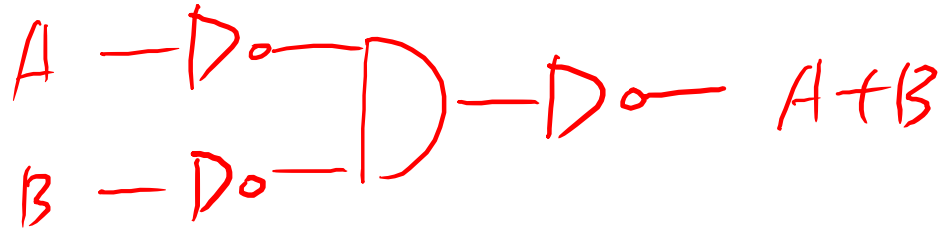
$\hookrightarrow \sum m_i$ (truth table)



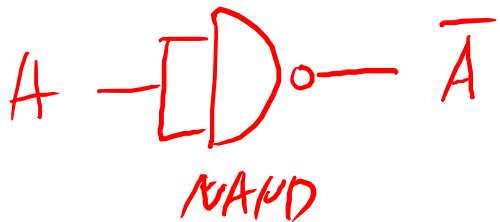
AND, NOT, OR

Universal Logic gate

- OR gate can be expressed by NOT and AND gates $\rightarrow$ {AND, NOT} is universal gate set



- AND, NOT gates can be expressed by NAND gate $\rightarrow$ NAND gate is universal logic gate



- NOR gate is universal logic gate as well

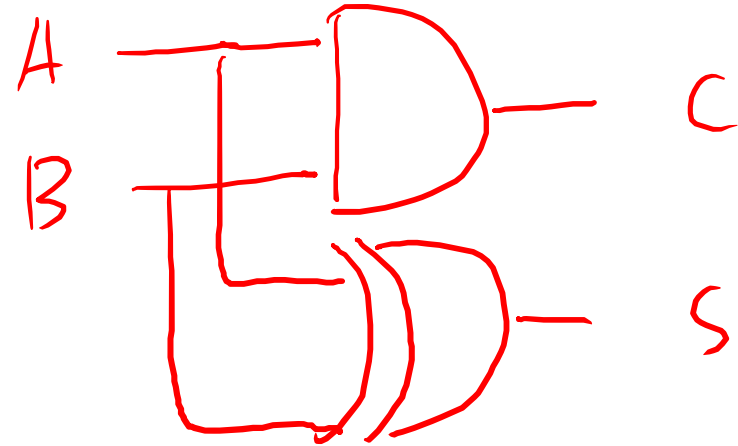
Example) Half-Adder

• $A+B = ?$

- $0 + 0 = 00$
- $0 + 1 = 01$
- $1 + 0 = 01$
- $1 + 1 = 10$

A	B	C	S
0	0	0	0
0	1	0	1
1	0	0	1
1	1	1	0

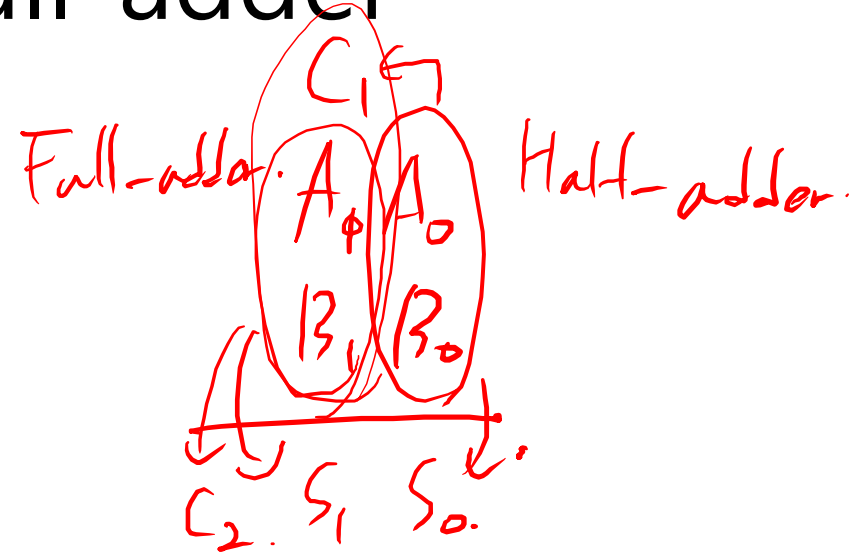
↑ ↑
AND XOR



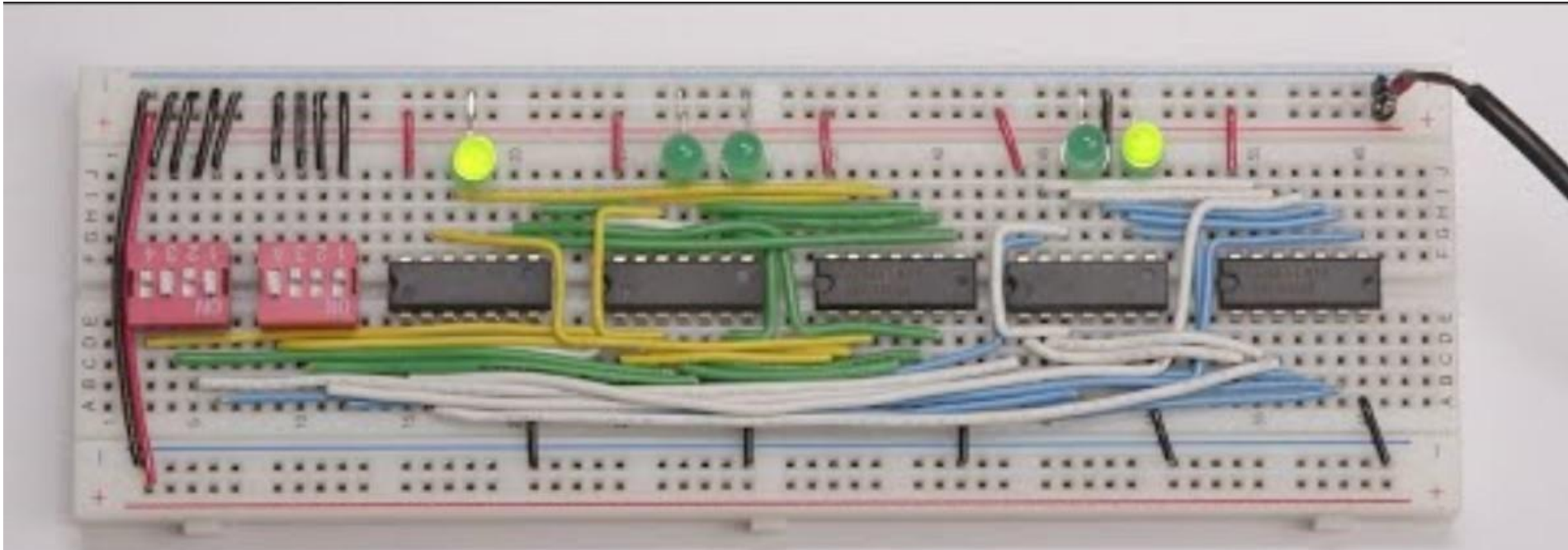
Example) Full-adder

- $A_1A_0 + B_1B_0 = ?$ $X_2X_1X_0$

- $A_0 + B_0 = C_1S_0$: Half-adder
- $A_1 + B_1 + C_1 = C_2S_1$: Full-adder



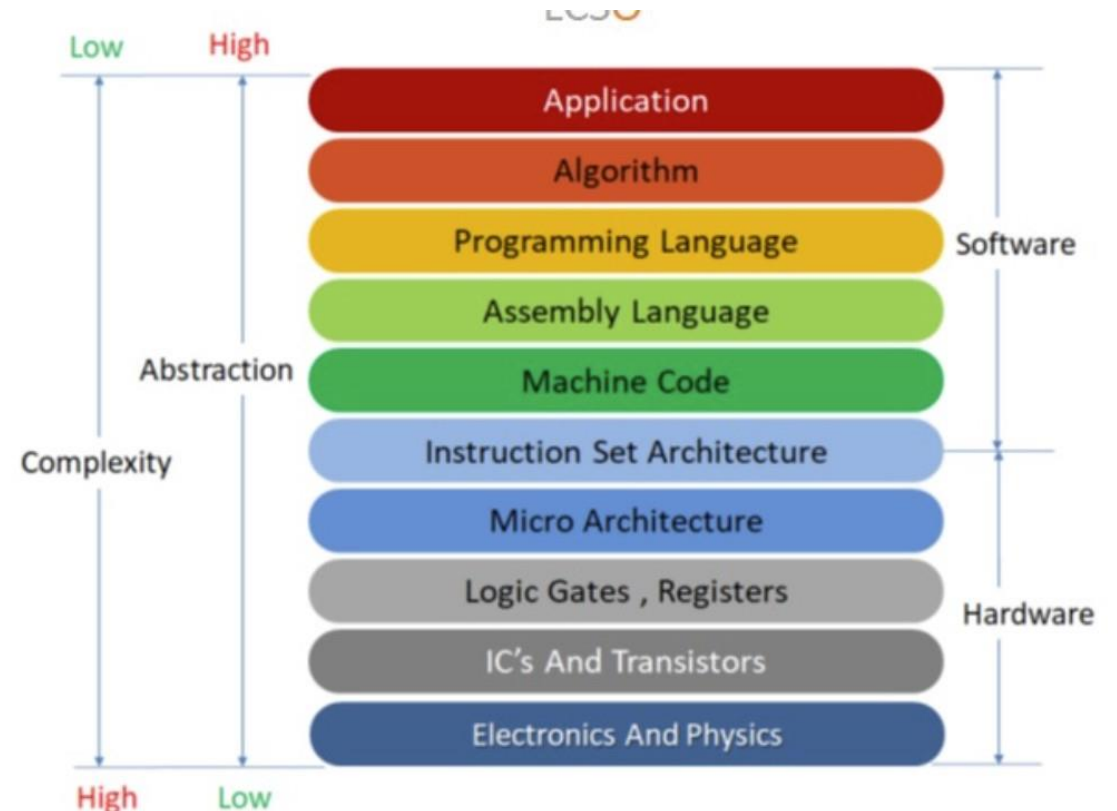
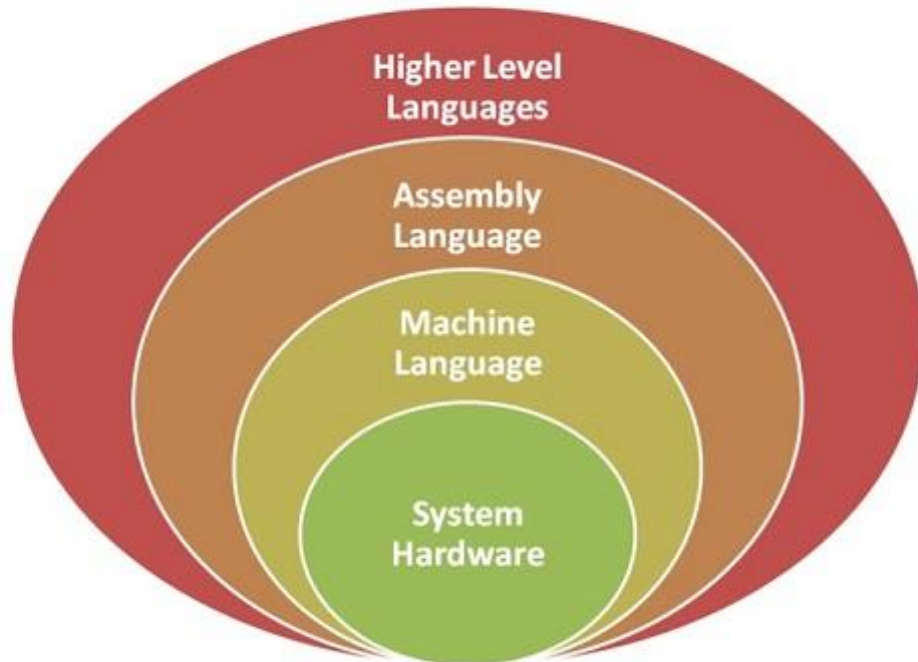
Example) IC circuit version



**How do computers
add numbers?**

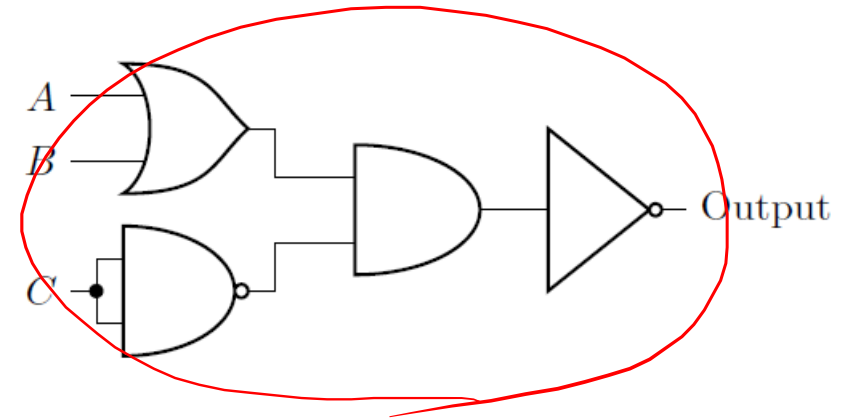
Program to hardware

- Modern programming paradigm has many abstraction layers.
- Some programming language still works in very low level - e.g.) Verilog for FPGA coding



Classical computing : summary

- What computers do at very low level → Logic gates
- Algebras for digital computers → Boolean algebra



- High-level programming language should be translated into low-level machine language to be executed.
- *What if our information units DO NOT follow Boolean algebra?*

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Audience Q&A Session

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Qubits

- Qubit = Quantum bit

Dirac notation

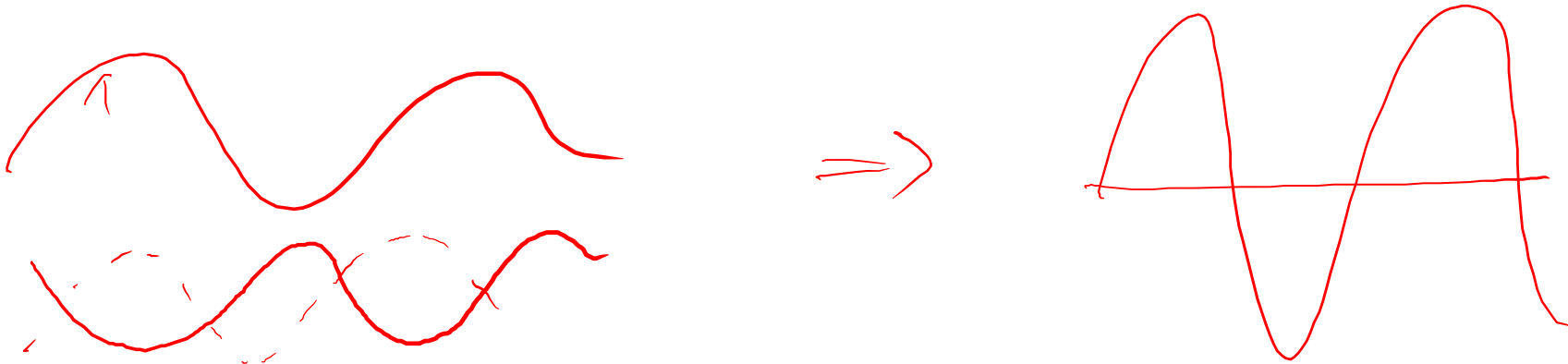


- Classical bit : 0 or 1 vs. Quantum bit : $|0\rangle$, $|1\rangle$

Rules for Qubits (1) : Superposition

중첩.

- Superposition is general physical phenomena (ex. Constructive/destructive interference of sound wave)



- Superposition in QM : allow multiple state vectors with different measurement outcomes!

$$\underline{\alpha |0\rangle + \beta |1\rangle}$$

$$\alpha, \beta \in \mathbb{C}$$

복소수.

Not only 0 or 1

- Qubit state can be described by numerous superposition state other than just 0 and 1

$$|\psi\rangle = \alpha|0\rangle + \beta|1\rangle$$

$|0\rangle$, $|1\rangle$

- One simple rule for a legal (single) qubit state: $|\alpha|^2 + |\beta|^2 = 1$

$$\alpha = a + bi$$

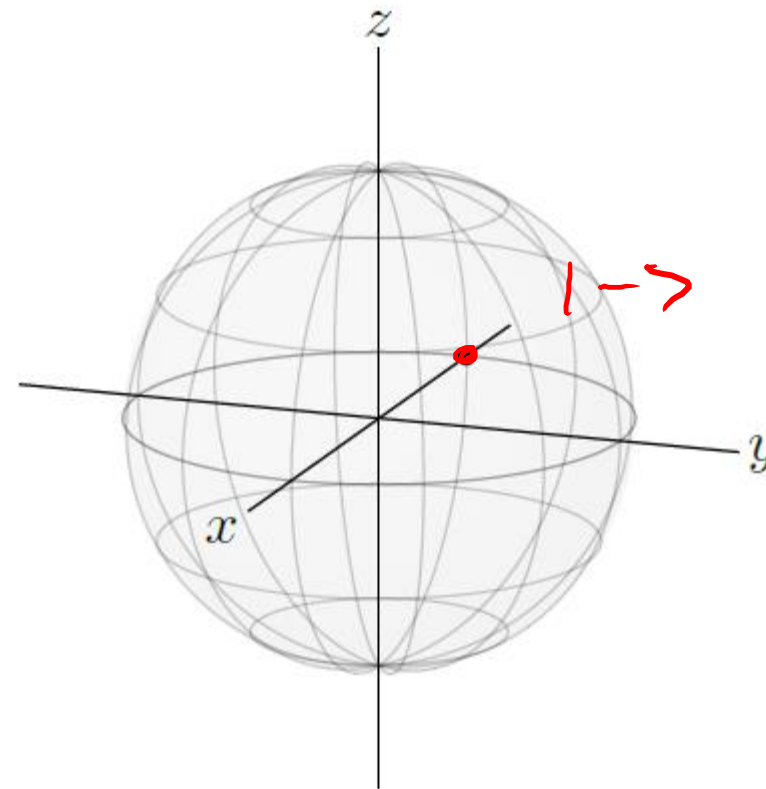
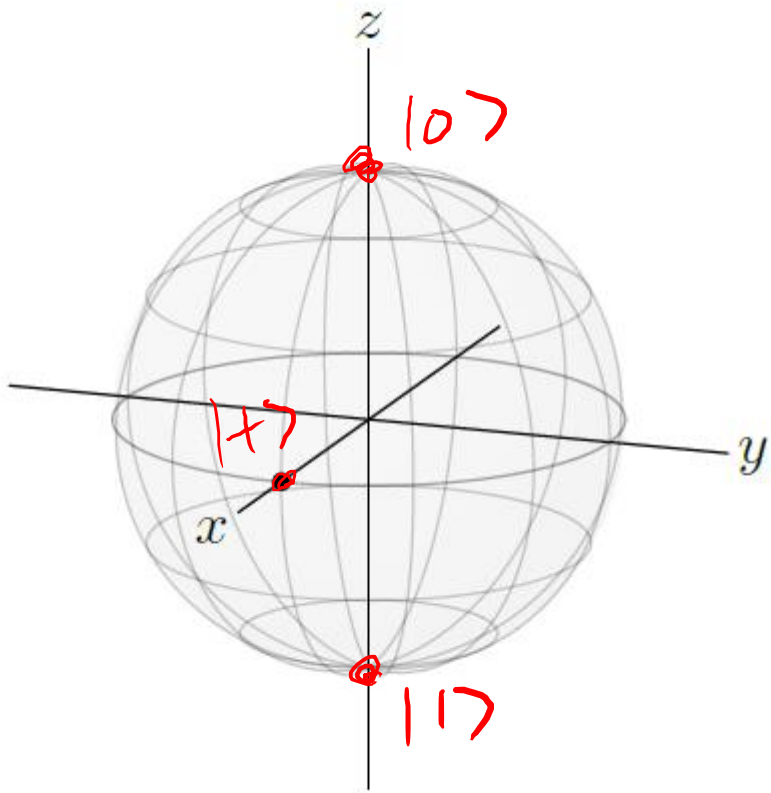
$$|\alpha|^2 = a^2 + b^2$$

Not only 0 or 1

$$\alpha = \beta = \frac{1}{\sqrt{2}}$$

$$\alpha = \frac{1}{\sqrt{2}}, \beta = -\frac{1}{\sqrt{2}}$$

- $|+\rangle = \frac{1}{\sqrt{2}}(|0\rangle + |1\rangle), |-\rangle = \frac{1}{\sqrt{2}}(|0\rangle - |1\rangle)$

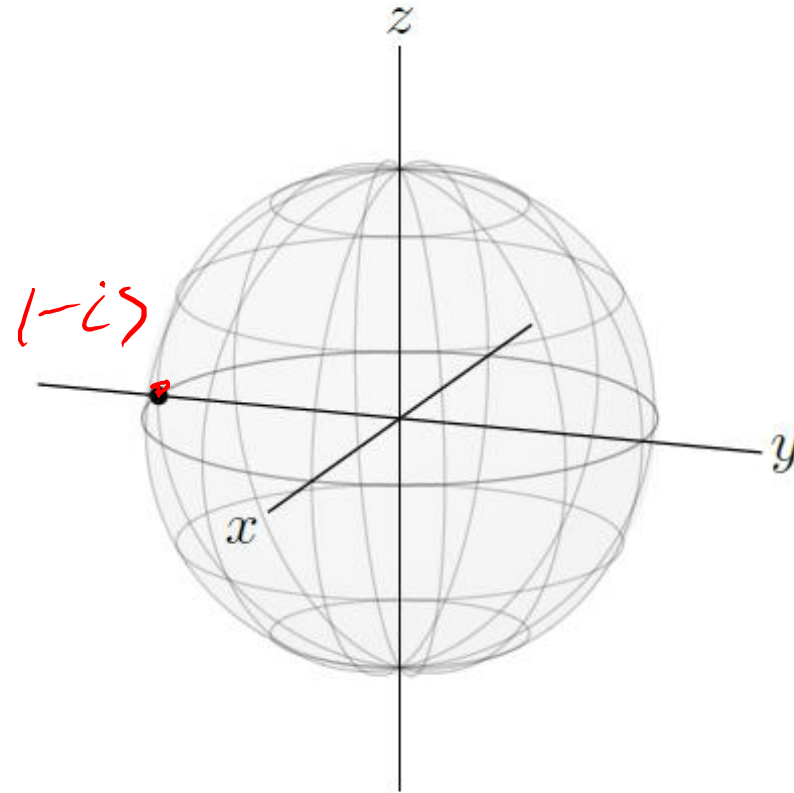
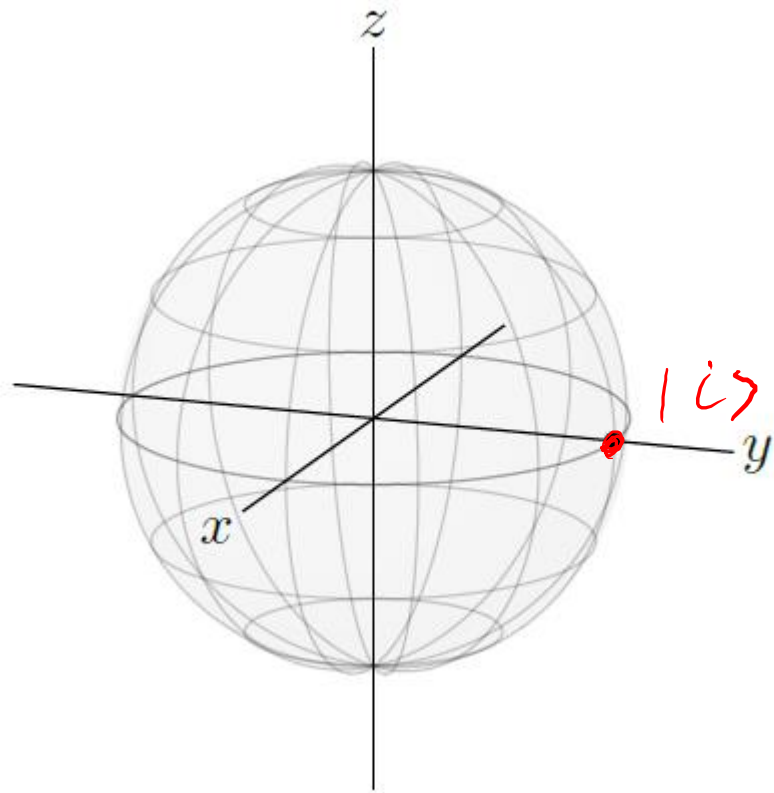


Not only 0 or 1

$$\alpha = \frac{1}{\sqrt{2}}, \beta = \frac{i}{\sqrt{2}}$$

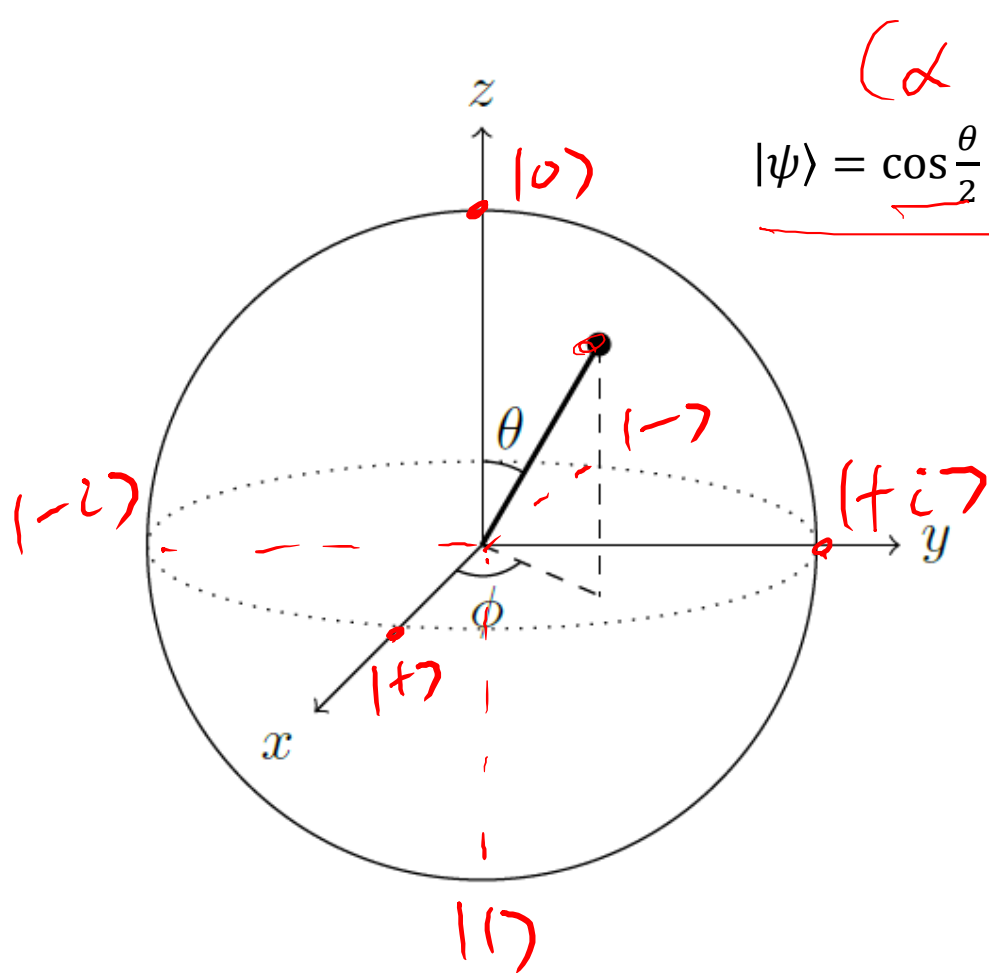
$$\alpha = \frac{1}{\sqrt{2}}, \beta = -\frac{i}{\sqrt{2}}$$

- $\underline{|i\rangle} = \frac{1}{\sqrt{2}}(|0\rangle + i|1\rangle), \underline{|-i\rangle} = \frac{1}{\sqrt{2}}(|0\rangle - i|1\rangle)$



Not only 0 or 1

- Arbitrary single qubit states can be mapped on to Bloch sphere



$$(\alpha, \beta) \leftrightarrow (\theta, \phi)$$
$$|\psi\rangle = \cos\frac{\theta}{2}|0\rangle + \sin\frac{\theta}{2}e^{i\phi}|1\rangle$$

Vector representation of qubits

ket
↓

- $|\psi\rangle = \alpha|0\rangle + \beta|1\rangle \rightarrow |\psi\rangle = \begin{pmatrix} \alpha \\ \beta \end{pmatrix}$

- $|0\rangle = \begin{pmatrix} 1 \\ 0 \end{pmatrix}, |1\rangle = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$

$$|+\rangle = \begin{pmatrix} \frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} \end{pmatrix}$$

bra
↓

- $\langle\psi| = (\alpha^* \quad \beta^*)$

Distance between qubit states

- How similar are two qubit states?

$$|\chi\rangle = \alpha|0\rangle + \beta|1\rangle = \begin{pmatrix} \alpha \\ \beta \end{pmatrix}$$

$$|\chi'\rangle = \begin{pmatrix} \alpha' \\ \beta' \end{pmatrix}$$

$$|\langle \chi | \chi' \rangle|^2 = \left| \begin{pmatrix} \alpha^* & \beta^* \end{pmatrix} \begin{pmatrix} \alpha' \\ \beta' \end{pmatrix} \right|^2 = \left| \alpha^* \alpha' + \beta^* \beta' \right|^2$$

$$|0\rangle = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$|1\rangle = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$\langle 0 | 1 \rangle = \begin{pmatrix} 1 & 0 \end{pmatrix} \begin{pmatrix} 0 \\ 1 \end{pmatrix} = 0.$$

$$0 \leq \leq 1$$

Fidelity

Rules for Qubits (2) : Measurement <+|->=0

- Quantum measurement on qubits

$$\underline{|\psi\rangle = \alpha|0\rangle + \beta|1\rangle} \rightarrow \begin{matrix} 0, 1 \\ |0\rangle \text{ or } |1\rangle \\ \text{2가지!} \end{matrix} \quad \begin{matrix} |x\rangle, |y\rangle \\ \hline |+\rangle, |-\rangle \end{matrix}$$

- {

i) $P_0 = |\alpha|^2$, $P_1 = |\beta|^2$ 확률들을 잰다.

ii) 재검증하네.

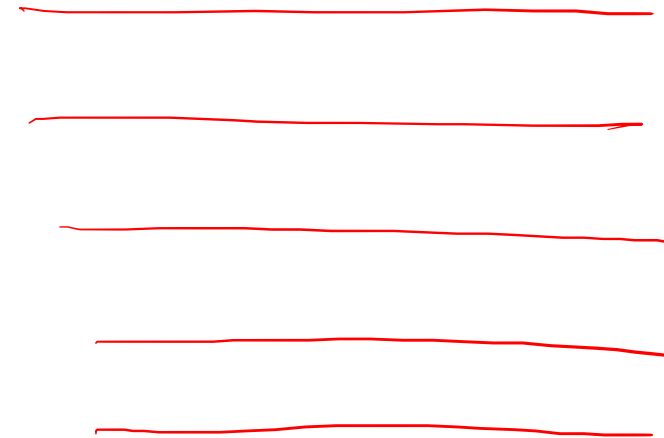
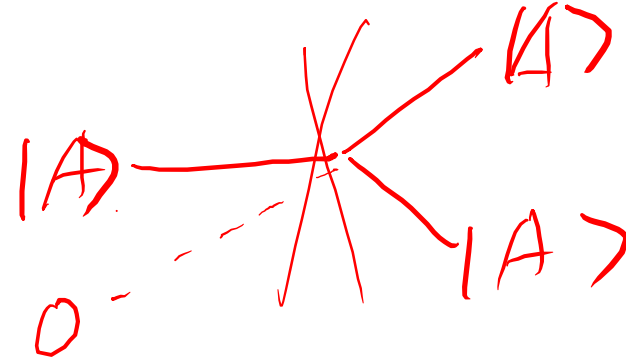
iii) $|\psi\rangle$ $\mapsto$ $|0\rangle$ / $|1\rangle$ 붕괴, 변환됨.

$\left\{ \begin{array}{l} P_x = |\langle x | \psi \rangle|^2 \\ P_y = |\langle y | \psi \rangle|^2 \end{array} \right.$

Rules for Qubits (3) : No-cloning Theorem

- Quantum information cannot be copied (no fan-out)

$$\underline{|\psi\rangle} |0\rangle \not\rightarrow |\psi\rangle |\psi\rangle$$



Rules for Qubits (4) : More than one qubit

- Tensor product

- $|0\rangle \otimes |0\rangle = |0\rangle|0\rangle = |00\rangle$: Both qubits are in 0 state. Tensor product

$|00\rangle$
 $|00\rangle$

- Basis for two qubits : $\{|00\rangle, |01\rangle, |10\rangle, |11\rangle\}$

- $|\psi\rangle = c_{00}|00\rangle + c_{01}|01\rangle + c_{10}|10\rangle + c_{11}|11\rangle \rightarrow |c_{00}|^2 + |c_{01}|^2 + |c_{10}|^2 + |c_{11}|^2 = 1$

$\uparrow \quad \uparrow \quad \uparrow \quad \uparrow$
 $\frac{1}{2} \frac{1}{2}$

- Other relevant notations

- Binary to decimal : $|110\rangle = |6\rangle$ (little endian)

- Powers : $|0\rangle^{\otimes n} = |00 \dots 0\rangle$

Multi-qubit measurement

- Reminder : measuring $|\psi\rangle = \alpha|0\rangle + \beta|1\rangle$? $\rightarrow P_0 = |\alpha|^2, P_1 = |\beta|^2$

- Multi-qubit states : $\frac{1}{\sqrt{2}}|00\rangle + \frac{1}{2}|01\rangle + \frac{\sqrt{3}}{4}|10\rangle + \frac{1}{4}|11\rangle$.

$\downarrow$	$\downarrow$	$\downarrow$	$\downarrow$
$\frac{1}{2}$	$\frac{1}{4}$	$\frac{3}{16}$	$\frac{1}{16}$
00	01	10	11

Sequential Single-qubit Measurements

$$\frac{1}{\sqrt{2}}|00\rangle + \frac{1}{2}|01\rangle + \frac{\sqrt{3}}{4}|10\rangle + \frac{1}{4}|11\rangle.$$

Entanglement

- Product state
- Entangled state

Bell states

$$|\Phi^+\rangle = \frac{1}{\sqrt{2}} (|00\rangle + |11\rangle),$$

$$|\Phi^-\rangle = \frac{1}{\sqrt{2}} (|00\rangle - |11\rangle),$$

$$|\Psi^+\rangle = \frac{1}{\sqrt{2}} (|01\rangle + |10\rangle),$$

$$|\Psi^-\rangle = \frac{1}{\sqrt{2}} (|01\rangle - |10\rangle).$$

Qubits : summary

- Rules for qubits:
 1. Superposition : $|\psi\rangle = \alpha|0\rangle + \beta|1\rangle$
 2. Measurement
 3. No-cloning theorem
 4. Multi-qubit representation
- Algebra for qubits : Linear algebra

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Audience Q&A Session

① Start presenting to display the audience questions on this slide.

Quantum gate

- Quantum gates transfer one qubit state to other (c.f. logic gates)

input qubit $\xrightarrow{\text{Quantum Gate.}} \alpha', \beta'$ output qubit.

$|\psi\rangle = \alpha|0\rangle + \beta|1\rangle$

$|\alpha|^2 + |\beta|^2 = 1.$

A	$\bar{A}$
0	1
1	0

- Quantum gates on superposition states

$$G|0\rangle = |\psi_0\rangle$$

$$G|1\rangle = |\psi_1\rangle$$

$$G(\alpha|0\rangle + \beta|1\rangle)$$

$$= \alpha(G|0\rangle) + \beta(G|1\rangle)$$

$$= \alpha|\psi_0\rangle + \beta|\psi_1\rangle$$

$ A\rangle$	output.
$ 0\rangle$	$ \psi_0\rangle = \begin{pmatrix} \alpha \\ \beta \end{pmatrix}$
$ 1\rangle$	$ \psi_1\rangle = \begin{pmatrix} \alpha' \\ \beta' \end{pmatrix}$

Single qubit quantum gates

- Identity gate

$$I|0\rangle = |0\rangle,$$
$$I|1\rangle = |1\rangle.$$

- Pauli X gate (NOT gate)

$$X|0\rangle = |1\rangle,$$
$$X|1\rangle = |0\rangle.$$

$$X \underline{|+\rangle} = X \left(\frac{1}{\sqrt{2}} |0\rangle + \frac{1}{\sqrt{2}} |1\rangle \right) = \frac{1}{\sqrt{2}} |1\rangle + \frac{1}{\sqrt{2}} |0\rangle = \underline{|+\rangle}$$

Single qubit quantum gate

- Pauli Y gate

$$Y|0\rangle = i|1\rangle,$$

$$Y|1\rangle = -i|0\rangle.$$

in	out.
$ 0\rangle$	$i 1\rangle$
$ 1\rangle$	$-i 0\rangle$

- Pauli Z gate

$$Z|0\rangle = |0\rangle,$$

$$Z|1\rangle = -|1\rangle.$$

in	out
$ 0\rangle$	$ 0\rangle$
$ 1\rangle$	$- 1\rangle$

$$Z|+\rangle = Z\left(\frac{1}{\sqrt{2}}|0\rangle + \frac{1}{\sqrt{2}}|1\rangle\right) = \frac{1}{\sqrt{2}}|0\rangle - \frac{1}{\sqrt{2}}|1\rangle = |-\rangle$$

Single qubit quantum gate

- Phase gate (S gate)

$$Z = S^2$$

$$S|0\rangle = |0\rangle,$$

$$S|1\rangle = i|1\rangle.$$

$$\begin{array}{c|c} & \\ \hline |0\rangle & |0\rangle \\ |1\rangle & i|1\rangle \end{array}$$

- T gate (Magic gate)

$$S = T^2$$

$$T|0\rangle = |0\rangle,$$

$$T|1\rangle = \underbrace{e^{i\pi/4}}_{\sqrt{i}}|1\rangle.$$

$$\begin{array}{c|c} & \\ \hline |0\rangle & |0\rangle \\ |1\rangle & e^{i\pi/4}|1\rangle \end{array}$$

$$e^{i\theta} = \cos\theta + i\sin\theta$$

Matrix representation of Single qubit gate

- Results of single qubit gates should be also legal single qubit states

$$1 = |\alpha|^2 + |\beta|^2 = \underline{|\alpha'|^2 + |\beta'|^2}$$

$$G|0\rangle = g_{00}|0\rangle + g_{01}|1\rangle$$

$$G|1\rangle = g_{10}|0\rangle + g_{11}|1\rangle$$

$$G(\alpha|0\rangle + \beta|1\rangle) = \alpha G|0\rangle + \beta G|1\rangle = (g_{00}\alpha + g_{01}\beta)|0\rangle + (g_{10}\alpha + g_{11}\beta)|1\rangle = \alpha'|0\rangle + \beta'|1\rangle$$

$\xrightarrow{\alpha G|0\rangle + \beta G|1\rangle}$
 α' β'

$$\begin{pmatrix} \alpha' \\ \beta' \end{pmatrix} = \begin{pmatrix} g_{00} & g_{01} \\ g_{10} & g_{11} \end{pmatrix} \begin{pmatrix} \alpha \\ \beta \end{pmatrix}$$

$\downarrow$ output qubit $\downarrow$ 2x2 matrix $\downarrow$ input qubit

$$G(G^\dagger)^T = I$$

$\downarrow$ Unitary

Single qubit quantum gate

- Superposition of Quantum gates : $G = G_1 + G_2$

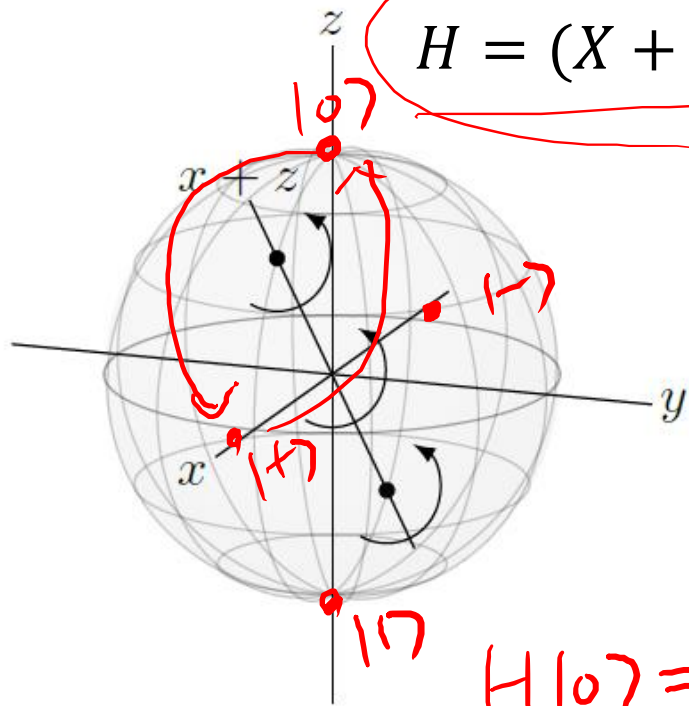
$$|0\rangle, |1\rangle \mapsto \alpha|0\rangle + \beta|1\rangle$$

$$G_1, G_2 \mapsto \underline{\underline{aG_1 + bG_2}}$$

$$(aG_1 + bG_2)|\psi\rangle = a(G_1|\psi\rangle) + b(G_2|\psi\rangle)$$

Single qubit quantum gate

- Hadamard gate (H gate)



$$H = (X + Z)/\sqrt{2}$$

$$\underline{H|0\rangle} = \frac{1}{\sqrt{2}} (|0\rangle + |1\rangle) = |+\rangle$$

$$H|1\rangle = \frac{1}{\sqrt{2}} (|0\rangle - |1\rangle) = |-\rangle$$

in	out
$ 0\rangle$	$ +\rangle$
$ 1\rangle$	$ -\rangle$

$$H|-\rangle = |1\rangle$$

$$H|0\rangle = \frac{1}{\sqrt{2}} (X+Z)|0\rangle = \frac{1}{\sqrt{2}} (X|0\rangle + Z|0\rangle) = \frac{1}{\sqrt{2}} (|1\rangle + |0\rangle) = |+\rangle$$

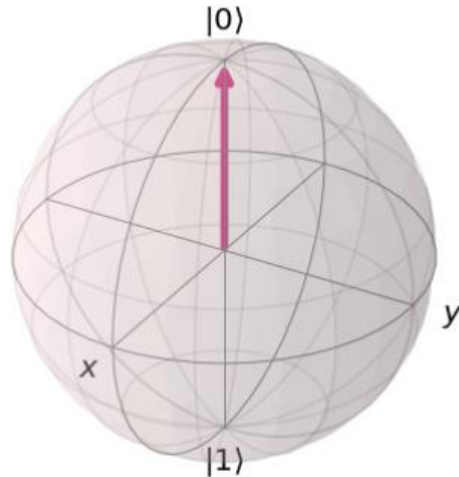
$$H|+\rangle = H\left(\frac{1}{\sqrt{2}}|0\rangle + \frac{1}{\sqrt{2}}|1\rangle\right) = \frac{1}{\sqrt{2}}|+\rangle + \frac{1}{\sqrt{2}}|-\rangle = |0\rangle$$

Single qubit quantum gate

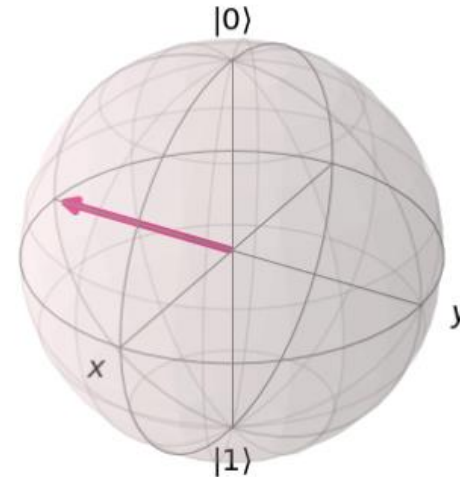
- Rotation X (Y, Z) : $R_x(\theta) = \cos^0 \frac{\theta}{2} I + i \sin^1 \frac{\theta}{2} X$

$$\theta = \pi$$

Before Applying RX Gate



After Applying RX Gate



- Any single qubit gate can be represented as rotation on the Bloch sphere

State initialization and measurement

↳ Non-unitary

- State initialization : reset qubit state into $|0\rangle$

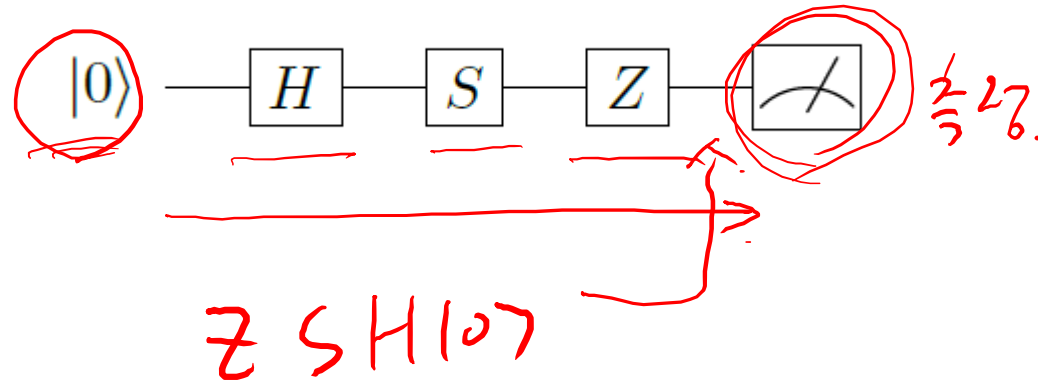
	G
$ 0\rangle$	$ 0\rangle$
$ 1\rangle$	$ 0\rangle$

$$\underline{G(\alpha|0\rangle + \beta|1\rangle)} = \underline{(\alpha + \beta)|0\rangle}$$

- State measurement : “collapse” qubit states into $|0\rangle$ or $|1\rangle$

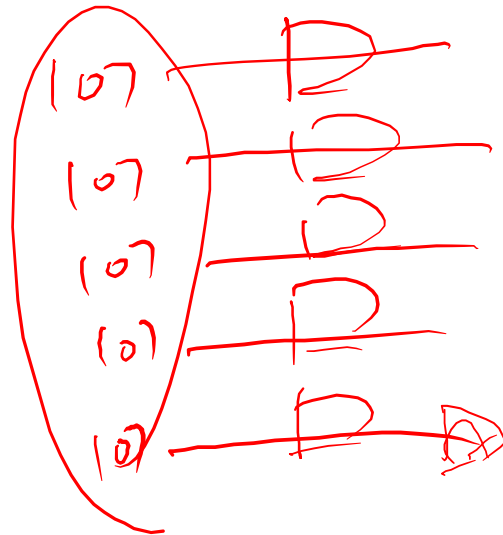
Quantum Circuit

- Alike classical logic circuit, quantum circuits consist of qubits and quantum gates.
- One difference is measurement operator, which did not exist in logic circuit.



Quantum gates on multi-qubits

- Single-qubit quantum gates on multi-qubit states



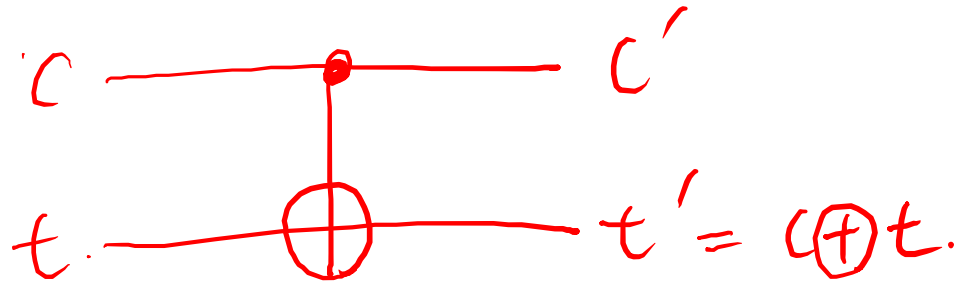
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Multi-qubit quantum gate

- Multi-qubit gate : Quantum gate acting on multiple qubits
 - c.f.) multi-bit logic gate : AND / OR
- Reversible, Unitary
- Can generate/eliminate quantum entanglement! (single qubit gates X)

Controlled- quantum gates

- Controlled NOT or CNOT



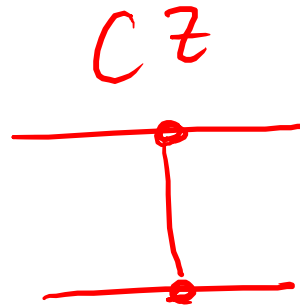
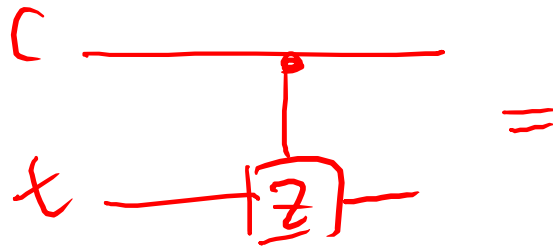
$c=0$

c	t	c'	t'
00	00	00	00
01	11	01	11
11	00	11	11
11	11	11	00

- CNOT vs. XOR

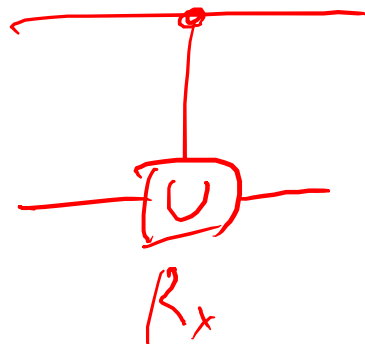
Controlled- quantum gates

- Controlled-Z gate



c	t	c'	t'
$ 0\rangle$	0	$ 0\rangle$	$ 0\rangle$
0	1	$ 0\rangle$	$ 1\rangle$
1	0	$ 1\rangle$	$ 0\rangle$
1	1	$- 1\rangle$	$ 1\rangle$

- Controlled-U gate

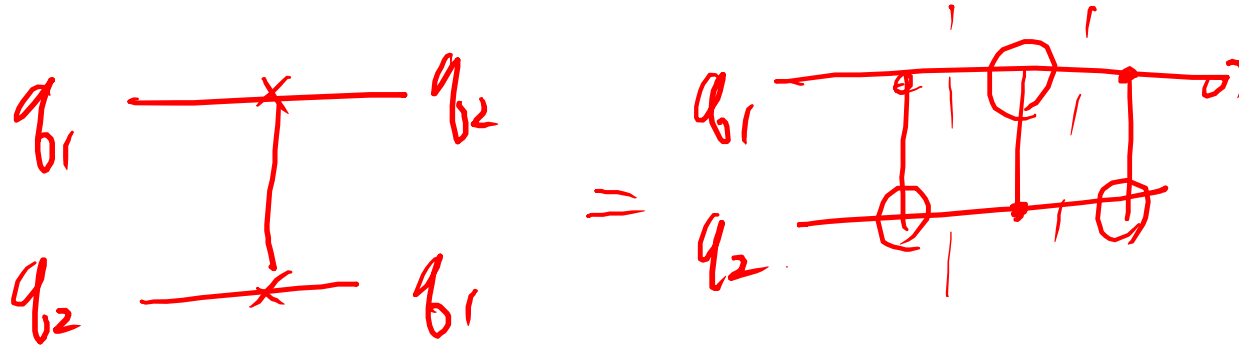


c	t	c'	t'
0	0	0	0
0	1	0	1
1	0	$ 1\rangle \otimes (U 0\rangle)$	
1	1	$ 1\rangle \otimes (U 1\rangle)$	

$$|1\rangle \otimes (U|1\rangle) = |1\rangle \otimes (-|1\rangle) = -|1\rangle \otimes |1\rangle$$

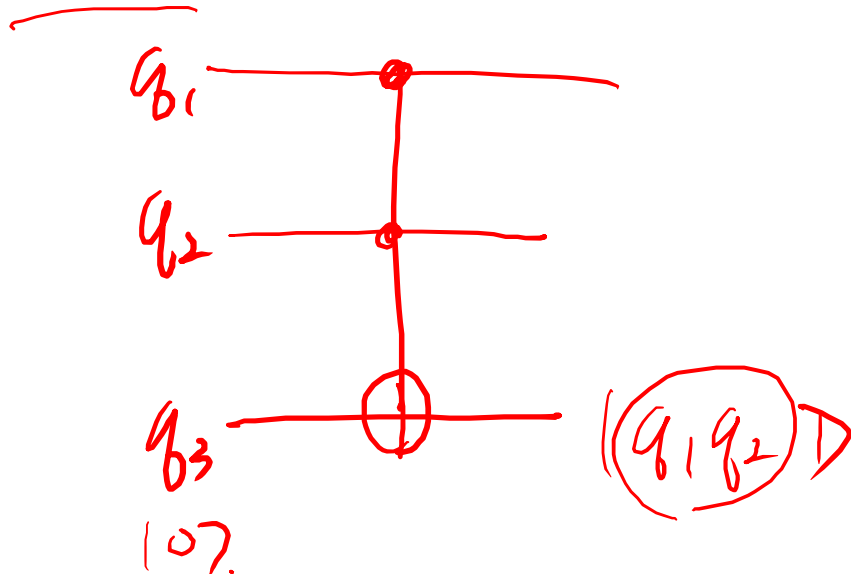
Other multi-qubit gates

- SWAP gate



- Toffoli gate (Quantum AND)

CCX



q_1	q_2	q_3	
0	0	0	
0	0	1	
0	1	0	
0	1	1	$\Rightarrow$
1	0	0	
1	0	1	
1	1	0	
1	1	1	

Hand-drawn truth table for the Toffoli gate. The table has columns for q_1 , q_2 , and q_3 . The first seven rows show all possible input combinations. The eighth row, where $q_1=1$, $q_2=1$, and $q_3=1$, is circled and has an arrow pointing to it, indicating the output is 1. The last row shows the output for the remaining input combinations, which is 0.

Universality of quantum gates

- One can build arbitrary quantum gates with finite set of quantum gates
- {CNOT, all single qubit gates}
- {CNOT, H, T} 
- {Toffoli, H, S}

Entangling qubits with quantum gates

- Bell state generation
- Greenberger–Horne–Zeilinger (GHZ) state

Quantum Gates & Circuits : Summary

- Quantum circuit is a sequence of abstracted quantum instructions.
 - Qubit initialization
 - Single qubit gates
 - Multi-qubit gates
 - Qubit measurements

Quiz!



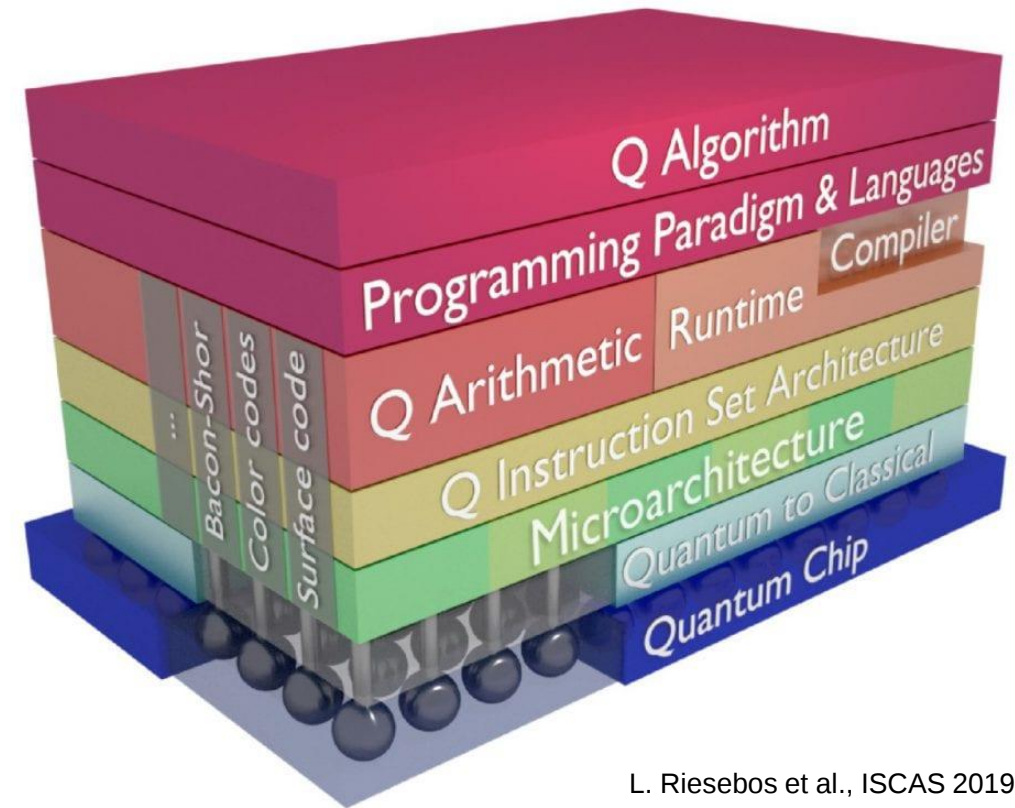
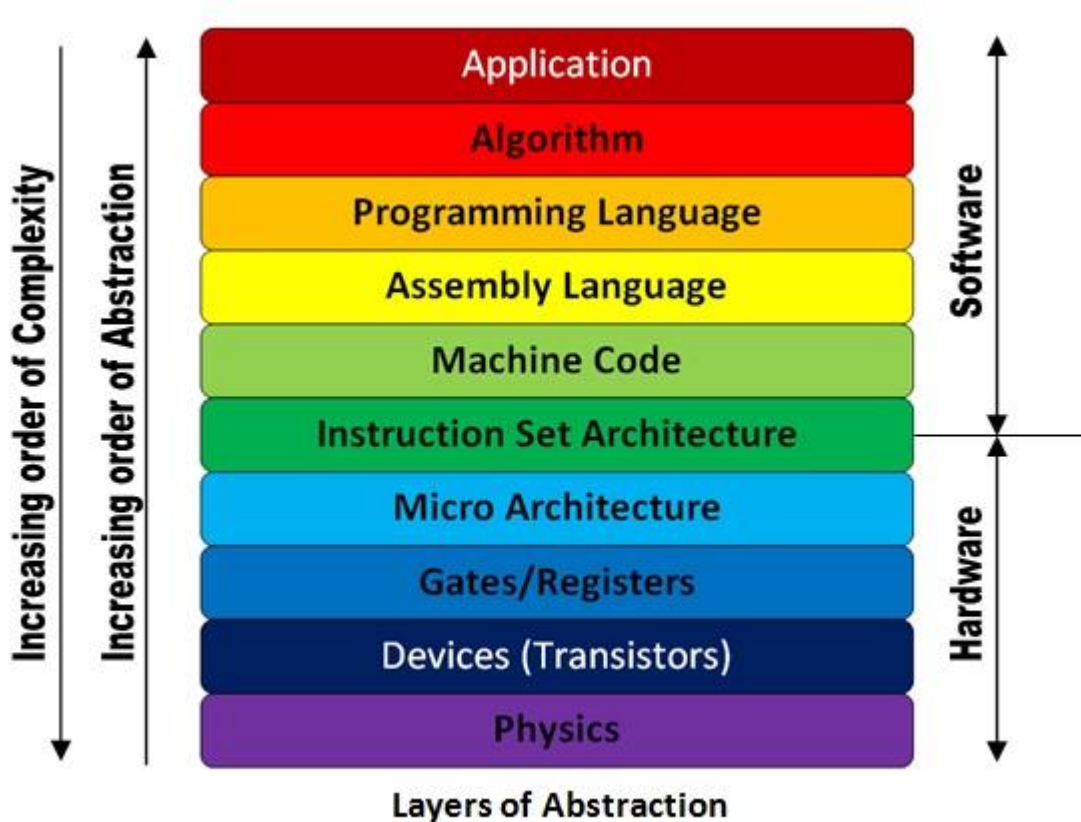
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Audience Q&A Session

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Computing architecture : Classical vs. Quantum

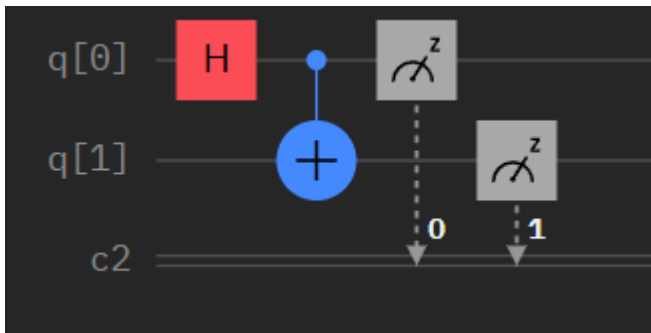


L. Riesebo et al., ISCAS 2019, pp. 1-4

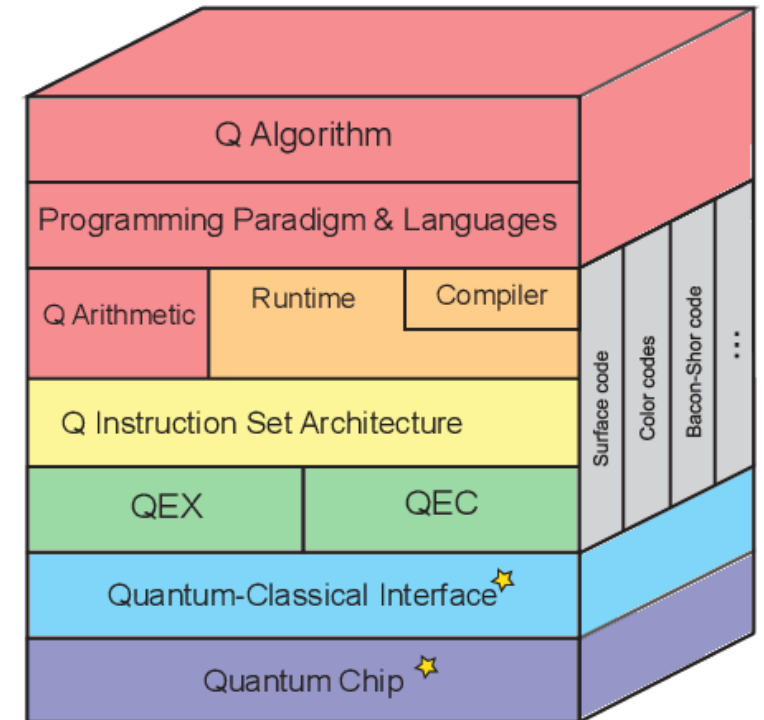
- Abstracted instructions for classical computer : Logic circuits
- Abstracted instructions for quantum computer : Quantum circuits

Quantum assembly language

- Programming languages designed for describing quantum instructions (circuits)
- OpenQASM, cQASM, Quil, Blackbird, Jaqal, etc.
- Mostly platform-agnostic (for gate-base QC)



```
1 OPENQASM 2.0;
2 include "qelib1.inc";
3
4 qreg q[2];
5 creg c[2];
6 h q[0];
7 cx q[0], q[1];
8 measure q[0] -> c[0];
9 measure q[1] -> c[1];
10
```



Toward higher level : Quantum SDKs

- Quantum SDK (Software Development Kits) helps users to write quantum programs (= quantum circuits)
- They provides useful features like:
 - Circuit optimizations
 - Gate decomposition
 - Simulation of quantum circuits on classical computers
 - Submit jobs to actual quantum computers on network
- **Mostly used in this winter school!**
- Not much abstraction has been made for quantum variables or functions. (Qint? Qfloat?)



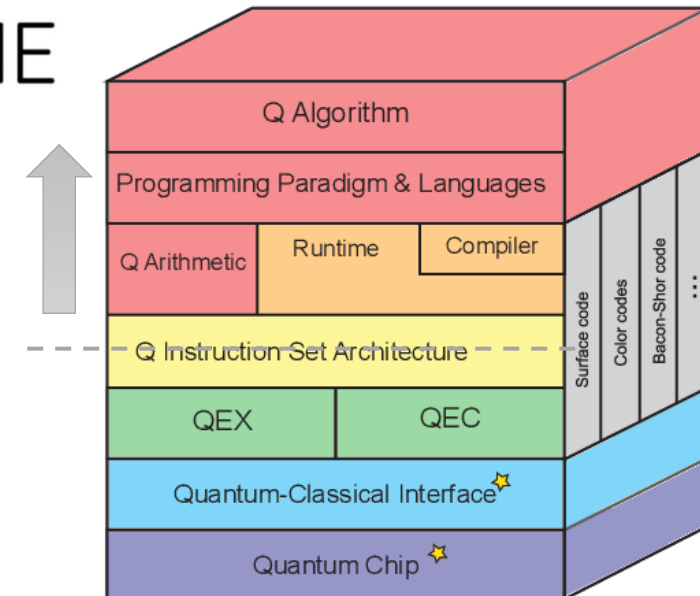
Qiskit



PENNYLANE



Cirq

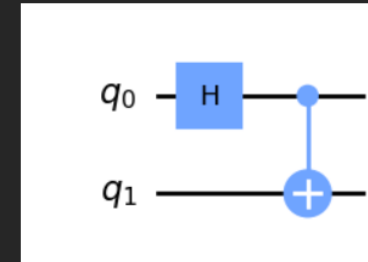


IBM Qiskit

- Open-source quantum SDK made by IBM researchers and collaborators.
 - Documentations : <https://docs.quantum.ibm.com/>
- Two main parts:
 - QuantumCircuit
 - Container for quantum circuit description
 - Pretty easy to use. See API reference.
 - Backend & Job
 - Backend objects represent quantum computer or simulator, which can execute QuantumCircuit contents
 - Each submission returns a Job object to track result asynchronously.

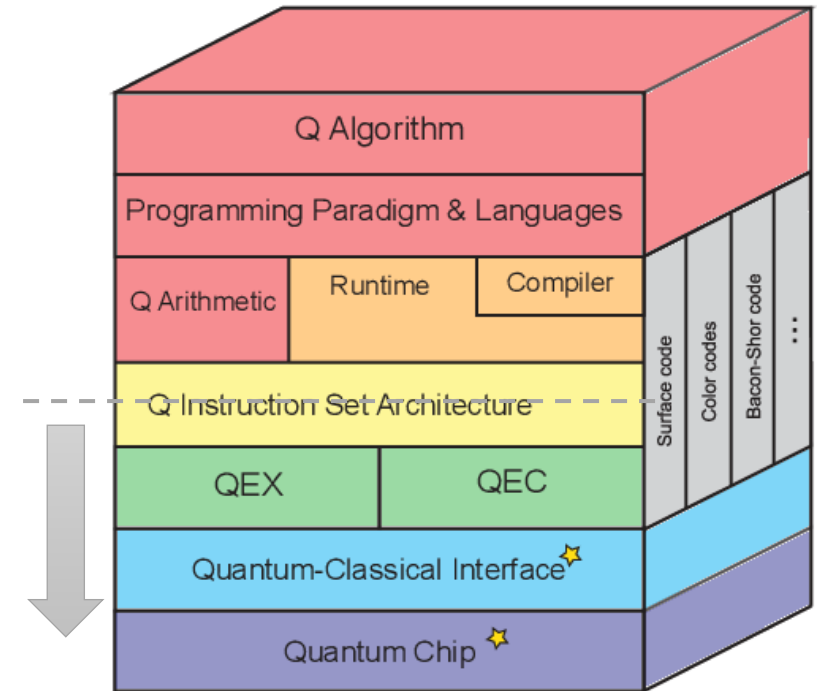
```
[1]: 1  from qiskit import QuantumCircuit
      2
      3  # Create a new circuit with two qubits (first argument) and two classical
      4  # bits (second argument)
      5  qc = QuantumCircuit(2)
      6
      7  # Add a Hadamard gate to qubit 0
      8  qc.h(0)
      9
     10  # Perform a controlled-X gate on qubit 1, controlled by qubit 0
     11  qc.cx(0, 1)
     12
     13  # Return a drawing of the circuit using Matplotlib ("mpl"). This is the
     14  # last line of the cell, so the drawing appears in the cell output.
     15  # Remove the "mpl" argument to get a text drawing.
     16  qc.draw("mpl")
```

Output:



Toward lower level : Control stack + Hardware

- To execute quantum program, instructions should be translated into actual physical sequence onto qubits.
 - Qubit mapping
 - Topological constraints resolving
 - Physical-gate decomposition
 - Physical-level optimization
- Not only hardware work, but also extensive software automation & optimization (like OS).



Toward lower level : Control stack + Hardware

Cloud data center provides
User interface/access, data storage, etc



Control Processor Layer
Drives control and measurement layer

Cryostat providing
Isolating environment



Control and measurement equipment
Drives signals to the qubits and measures the result



Qubits surrounded by
Connection wiring



IBM Quantum Two

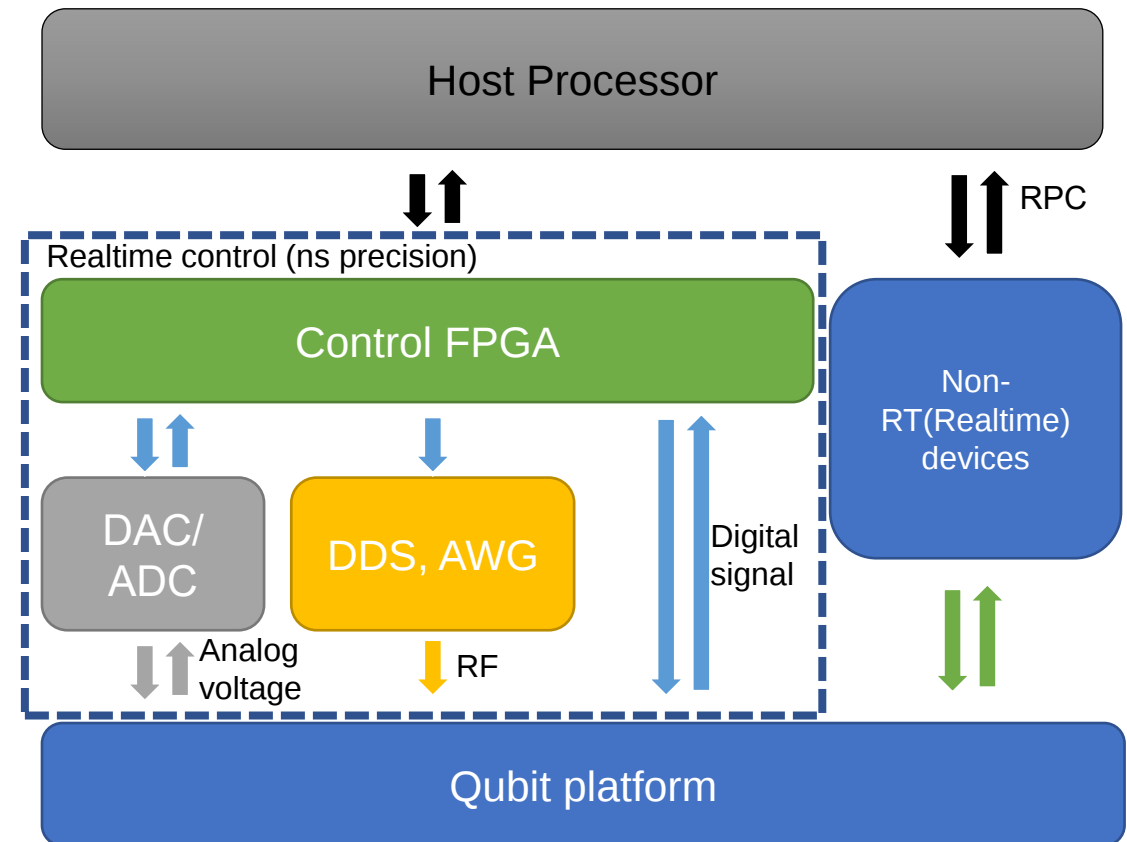
- Making qubits is hard, but controlling them very well is much harder.
- Calibration, exact control, tight scheduling, error mitigation, etc.

One example : IBM Quantum (Superconducting)



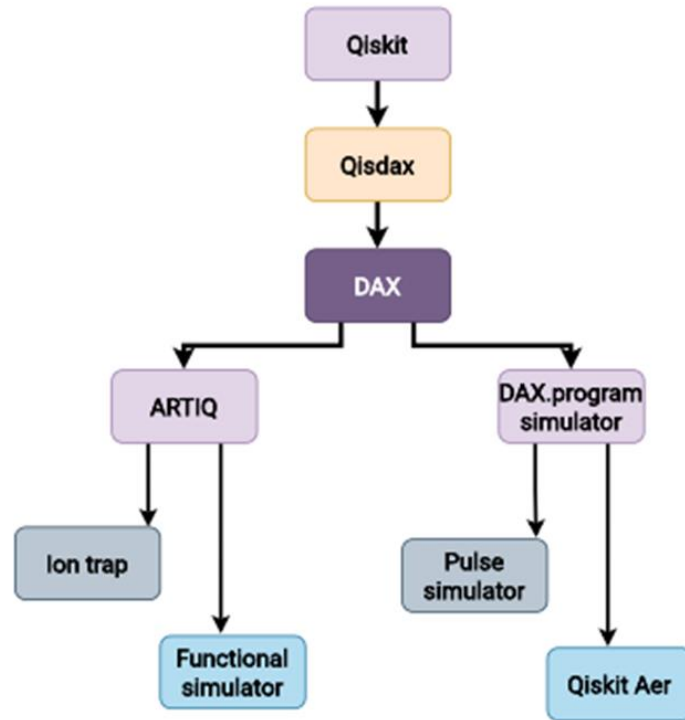
One example : Trapped-ion system

- Preparation stage
 - Check whether the trapped ion qubits are enough (if not, trap ions)
 - Check when the latest calibration was or whether it is correct (if not, re-calibrate them)
 - Compile control pulses (frequency, amplitude, pulse length) with calibration parameters
- Run stage
 - Initialize qubits states into $|0\rangle$ with a laser pulse
 - Apply control laser pulses with nano-second precision via FPGA
 - Perform qubit readout and store the result (image or photon counts) into classical register
 - (if possible) Check whether the whole process has gone well (no qubit lost, system drift, etc)
- Analyze stage
 - Retrieve stored register values and convert them into measurement results.



ARTIQ-DAX layer abstraction

QISDAX software stack



Qiskit

```
from qiskit import QuantumCircuit, execute
from qiskit.visualization import plot_histogram
from qiskit.providers.dax import DAX

dax = DAX.get_provider()
backend = dax.get_backend('dax_artiq_device')
backend.load_config("resources.toml")

qc = QuantumCircuit(2,2)
qc.h(0)
qc.cx(0, 1)

qc.measure([0, 1], [0, 1])

dax_job = execute(qc, backend, shots=1000)
result = dax_job.result()
counts = result.get_counts()
print(f'Result: {counts}')

print(qc)
qc.draw(output='mpl').show()
plot_histogram(counts).show()
```

Automatic Transpile

ARTIQ Code(Dax)

```
***
Program generated on  by Qisdax v.
***

from dax.program import *

class QisdaxProgram(DaxProgram, Experiment):

    def build(self):
        self._num_iterations = 1000
        self._num_qubits = 2
        self.update_kernel_invariants('_num_iterations', '_num_qubits')
        self._classical_regs = set()

    def run(self):
        # Check number of qubits
        if self._num_qubits > self.q.num_qubits:
            raise RuntimeError('Circuit requires more qubits than the system supports')

        # Run the kernel
        self._run()

    @kernel
    def _run(self):
        t0 = self.core.get_rtio_counter_mu()
        self._qiskit_kernel()

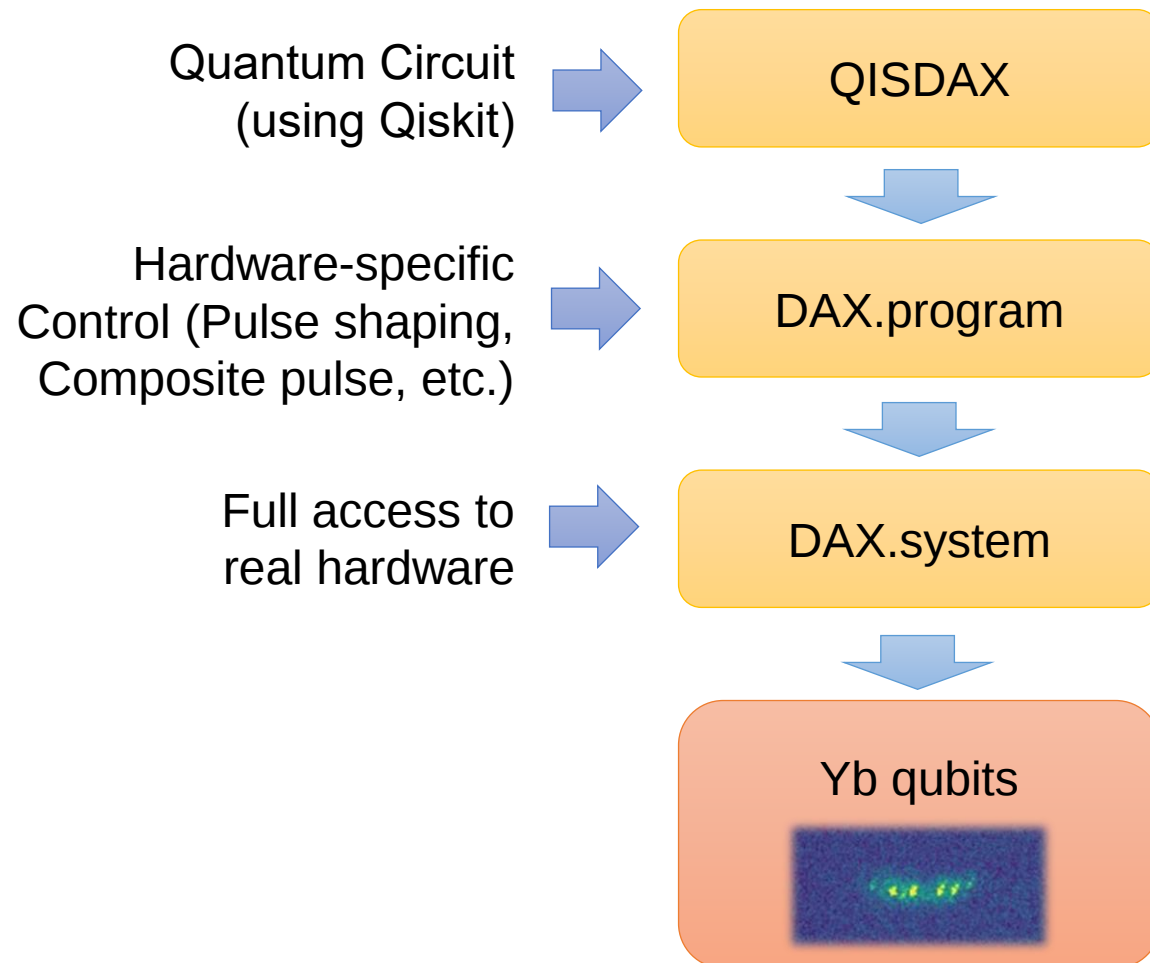
        self.core.wait_until_mu(now_mu())
        t1 = self.core.get_rtio_counter_mu()
        self.set_dataset("dt", self.core.mu_to_seconds(t1 - t0))

    @kernel
    def _qiskit_kernel(self):
        with self.data_context:
            for _ in range(self._num_iterations):
                self.core.reset()
                self.q.prep_0_all()

                self.q.h(0)
                pass
                self.q.cnot(0,1)
                pass
                with parallel:
                    with sequential:
                        self.q.m_z(0)
                        pass
                    self.q.store_measurements([0])
                    with sequential:
                        self.q.m_z(1)
                        pass
                    self.q.store_measurements([1])
```

- Recent work by NC State University enables Qiskit-based quantum circuit execution (QISDAX)
- We tested the QISDAX with our system simulator

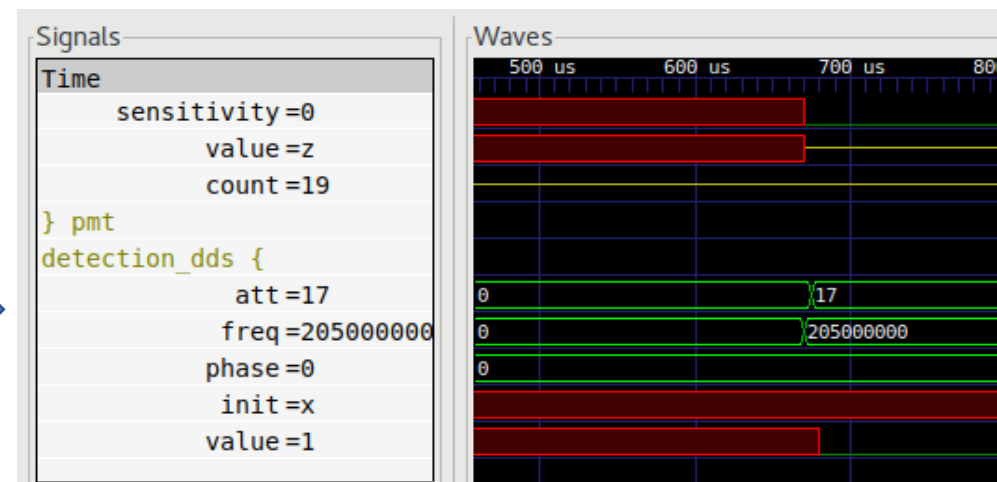
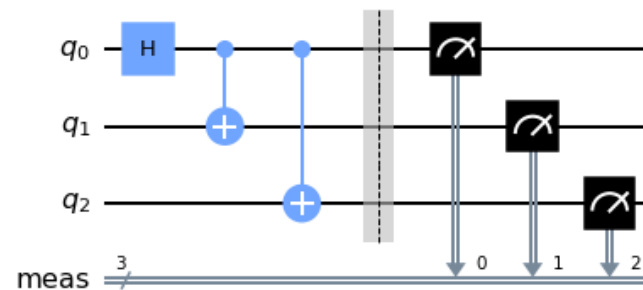
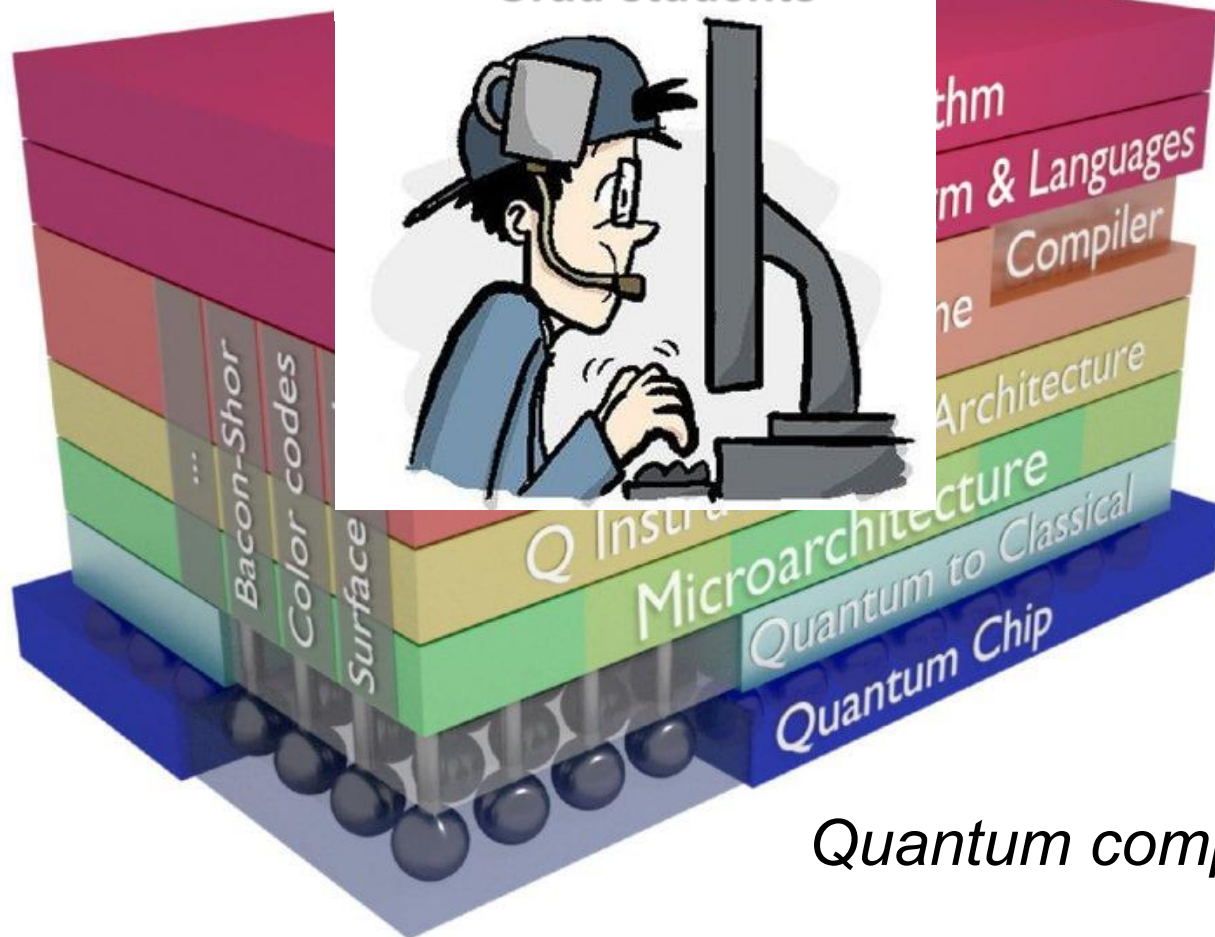
ARTIQ-DAX layer abstraction



- Multiple abstraction layer defines various access levels to the ion-trap QC device
- One could remotely submit jobs to the device via QISDAX or DAX.program
- Only functional simulator available now. (system simulator could be useful tho!)

Unfolding quantum circuits

Quick solution
= Grad students

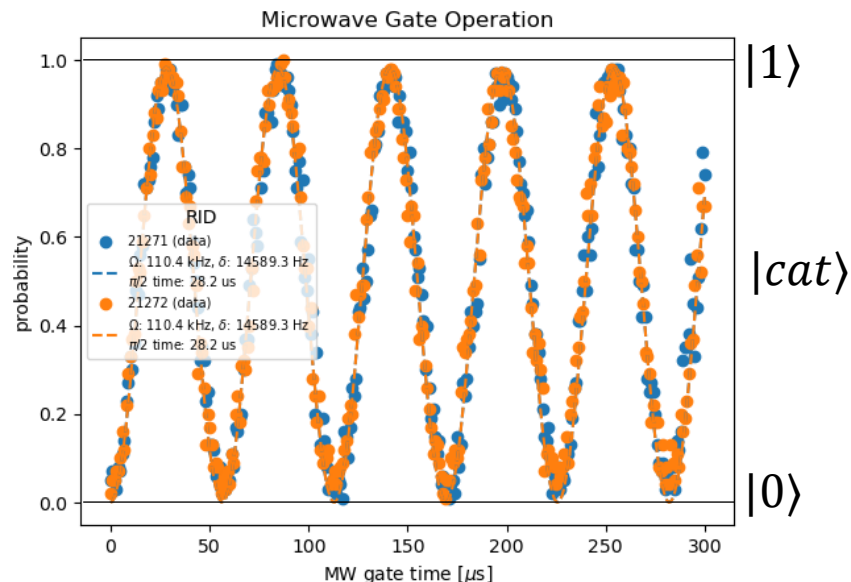


Hardware waveform

Quantum computing stack should be dynamic not static.

Quantum Engineering with Trapped Ions (QuETI) Lab @ SKKU

- Research Topic : Full-stack Ion-trap Quantum Computing
 - Build a system from bottom to top
 - Exciting research field for both quantum science and engineering!
 - Superposition ✓, Entangling operation comes soon!



Website: <https://iontrap.skku.edu>

Lab : 83292/83245

Office : 83212

We're looking for motivated undergrads & graduate students!

Contact info: Junki.kim.q@skku.edu

Quantum computing architecture : summary

- Programming language for quantum circuits : quantum assembly language
 - Mostly for gate-based quantum computers
- Quantum SDKs : handy utilities + functionalities for quantum coding
 - Not much abstraction made yet. The code is virtually the same with quantum circuit.
 - Useful to learn & code quantum algorithms
 - Examples : Qiskit, Cirq, PennyLane, etc.
- Hardware-dependent software stack : important and interesting engineering problem
 - Especially important for NISQ devices (limited performance)

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Audience Q&A Session

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